

# Física nolineal y smartphones

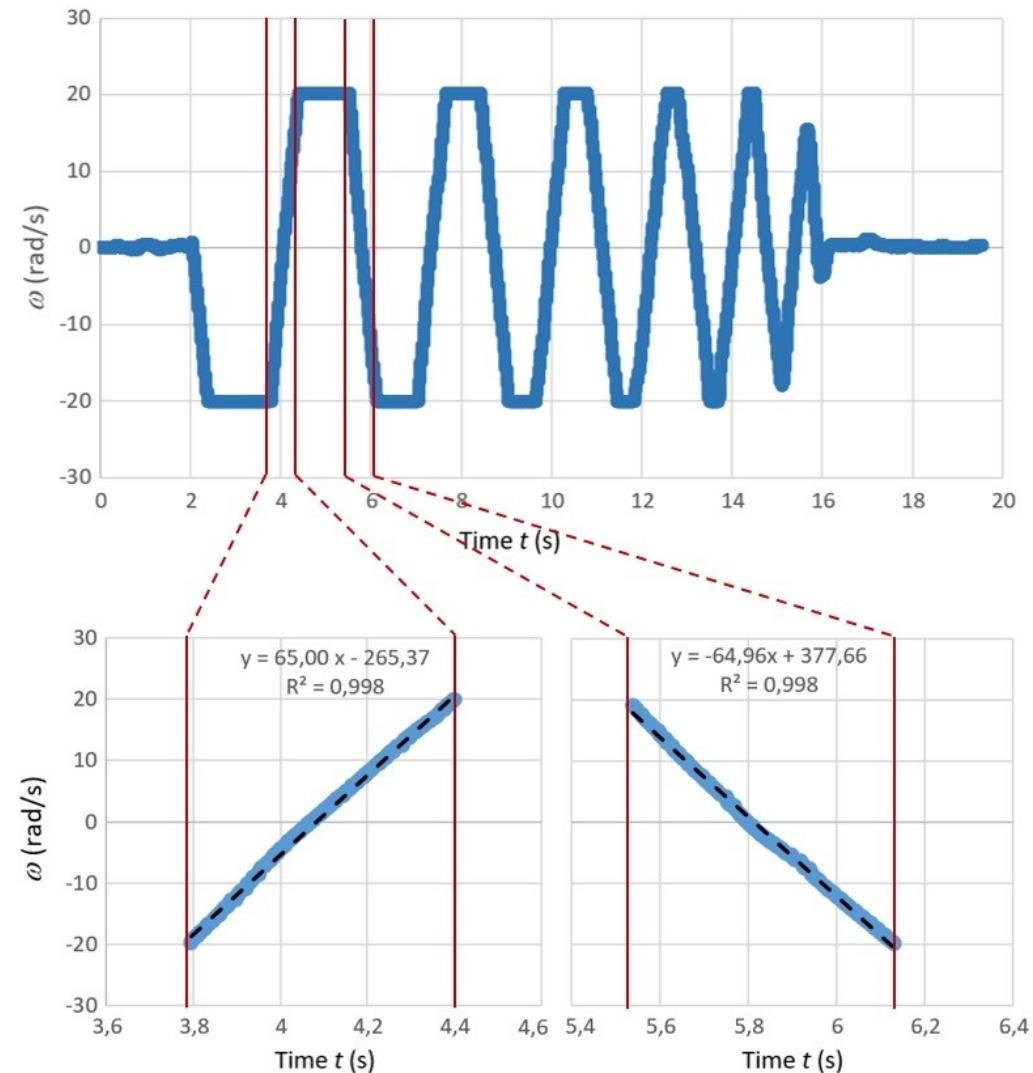
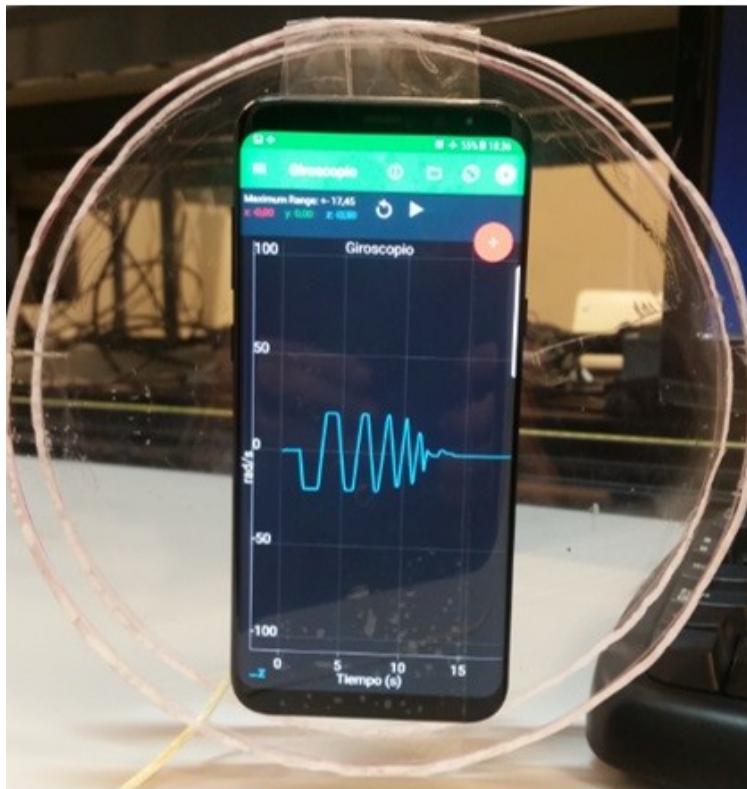
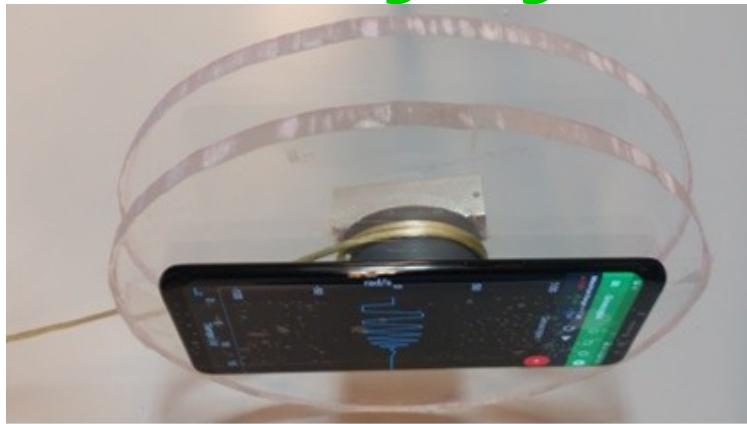
Arturo Martí

Universidad de la República

[marti@fisica.edu.uy](mailto:marti@fisica.edu.uy)

Seminario de Física nolineal,  
Junio, 2020

# T1: Analyzing the dynamics of a yoyo with a smartphone



**Isabel Salinas, MM, AM, Juan A. Monsoriu  
Physics Teacher 2020**

# T2: Péndulo físico + smartphone

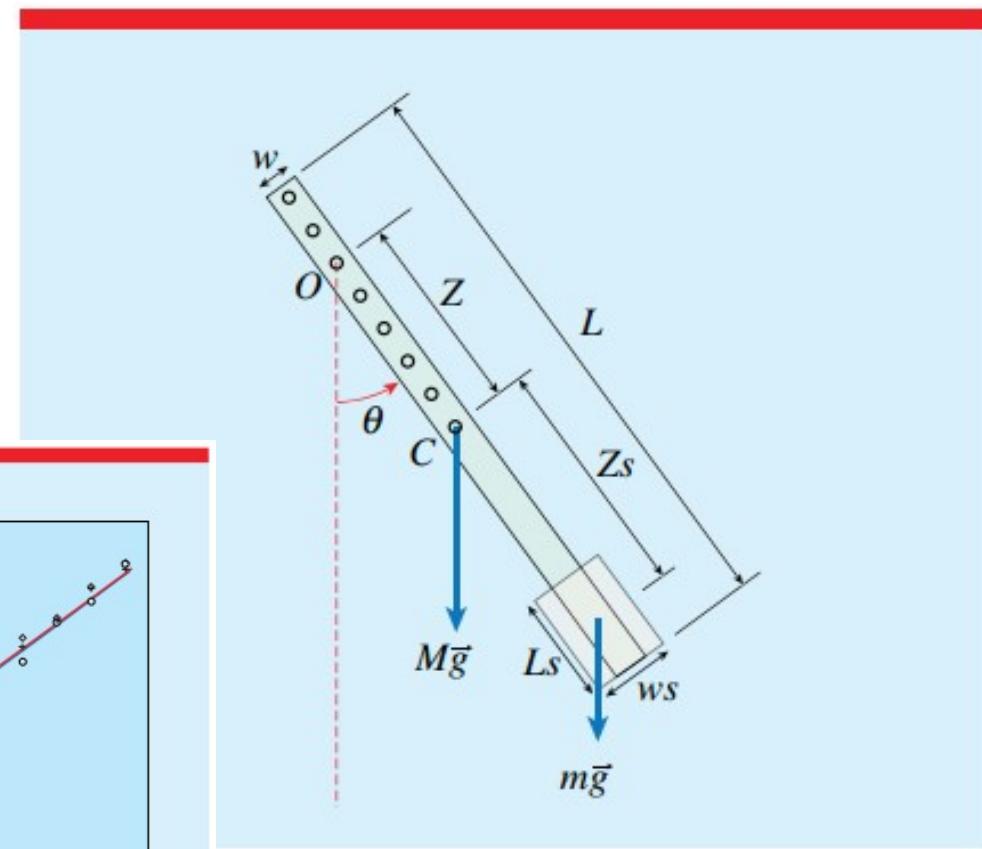
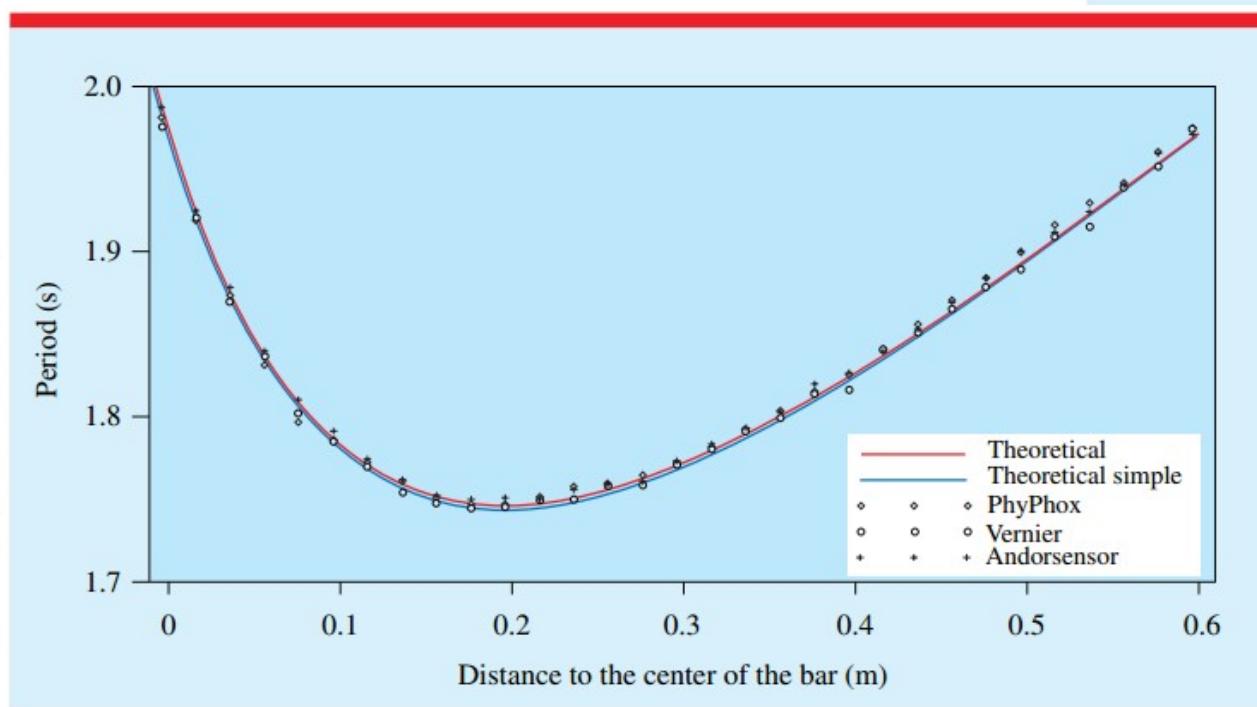
Phys. Educ. 55 (2020) 023004 (4pp)

FRONTLINE

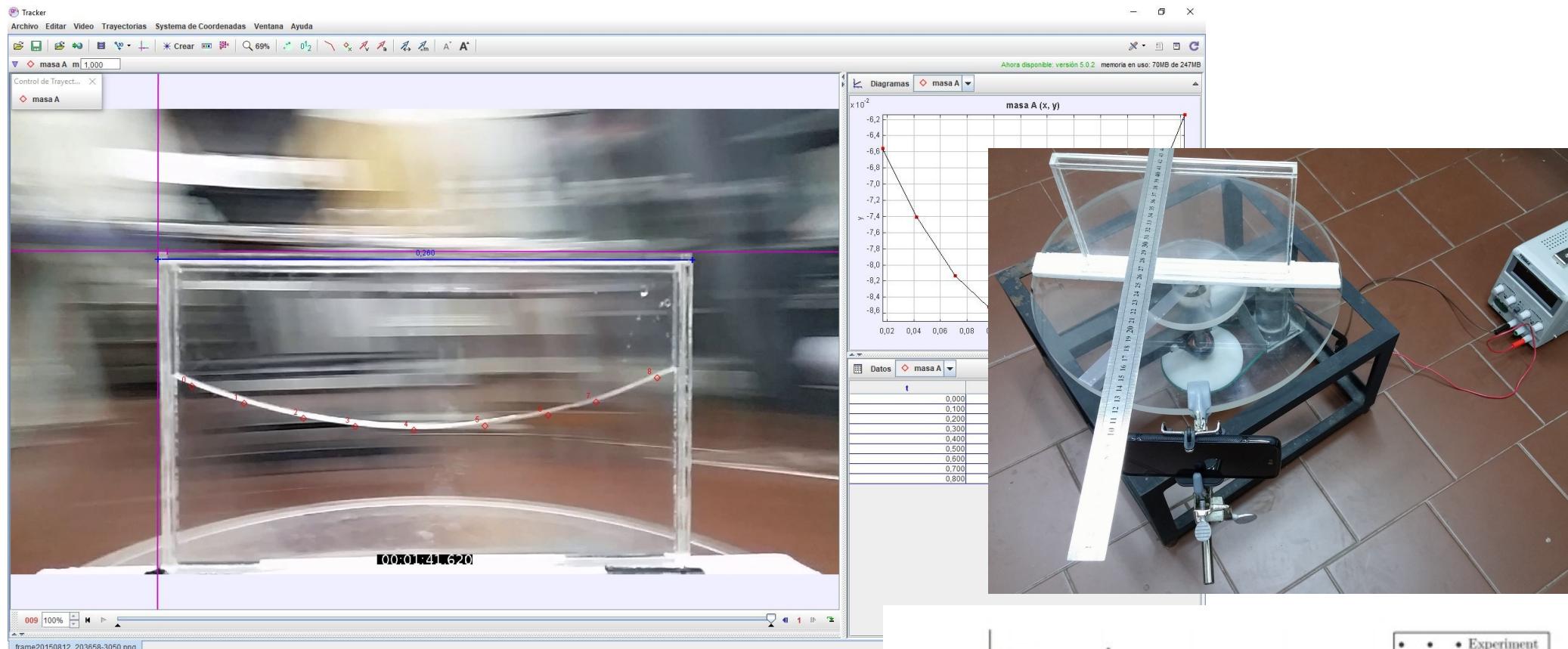
[iopscience.org/ped](https://iopscience.org/ped)

## Experimental analysis of a compound pendulum with variable suspension point

Martín Monteiro<sup>1,2</sup>, Cecilia Stari<sup>2</sup>, Cecilia Cabeza<sup>2</sup>  
and Arturo C Martí<sup>2</sup>



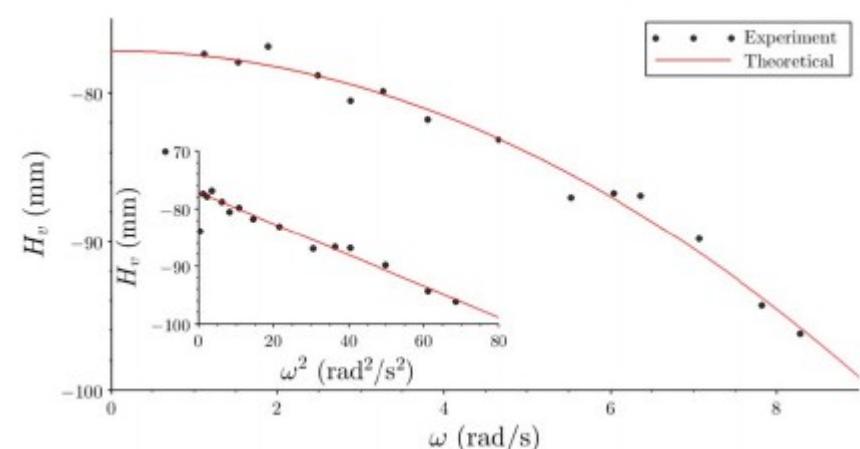
# T3: Smartphone + fluidos



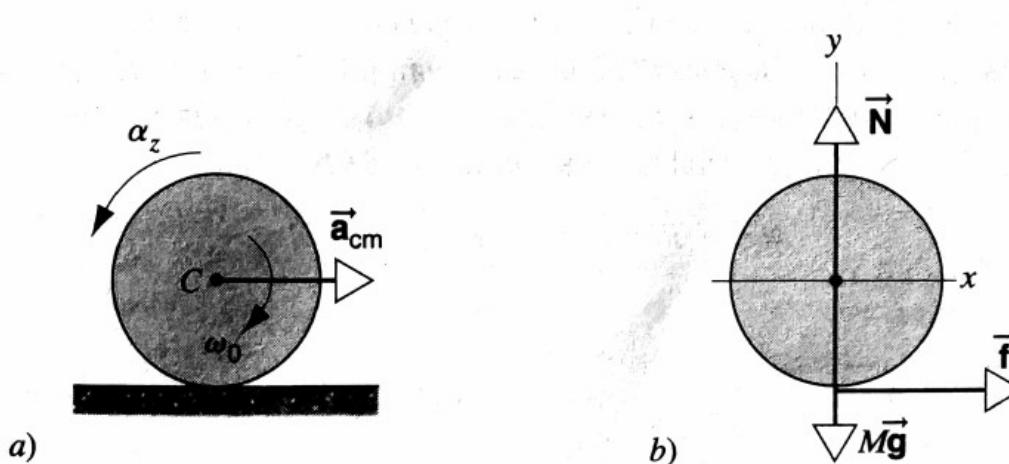
**Experimental analysis of the free surface of a liquid in a rotating frame**

Martín Monteiro<sup>1,2</sup> , Fernando Tornaría<sup>3</sup> and Arturo C Martí<sup>2,4</sup>

Eur. J. Phys. 41 (2020) 035005



# T4: Rodar + deslizar + video



a)

b)

**FIGURA 9-33.** Problema resuelto 9-12. a) El cilindro que gira se desliza inicialmente al rodar. b) Diagrama de cuerpo libre del cilindro.

Phys. Educ. 55 (2020) 013002 (5pp)

FRONTLINE

[iopscience.org/ped](https://iopscience.org/ped)

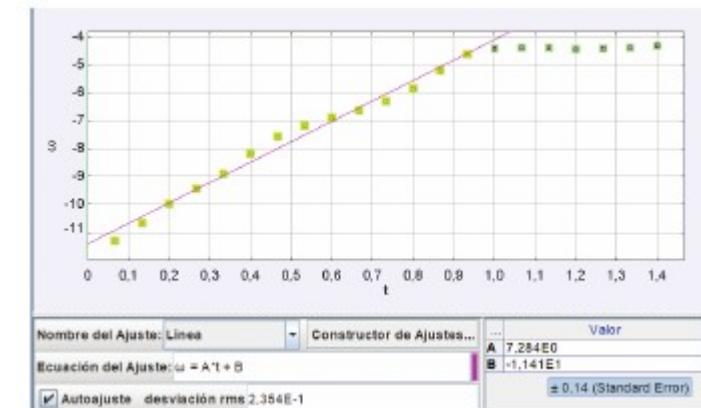
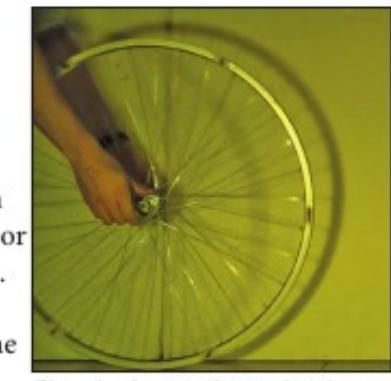
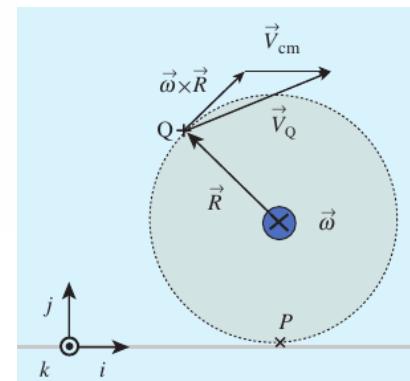
An experiment to address conceptual difficulties in slipping and rolling problems

Video-Based Analysis of the Transition from Slipping to Rolling

Álvaro Suárez and Daniel Baccino, CFE, Uruguay  
Arturo C. Martí, Universidad de la República, Uruguay

Phys. Teach. 58, 170 (2020);

Transición deslizamiento- rodadura  
Distribución de velocidades rígido  
(sistema de lab y relativo)  
Coeficiente estático vs dinámico  
Fuerza de rozamiento “acelera”

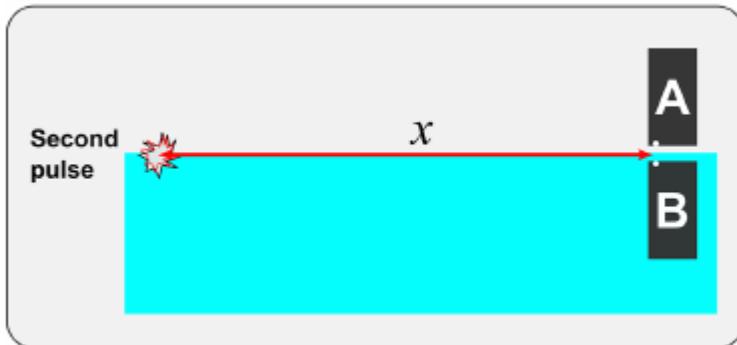


# T5: Acústica submarina

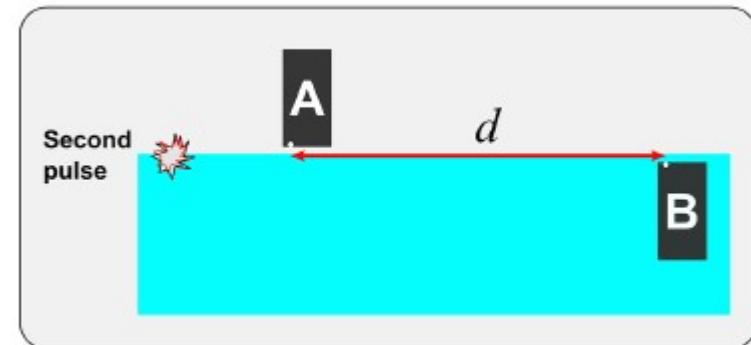
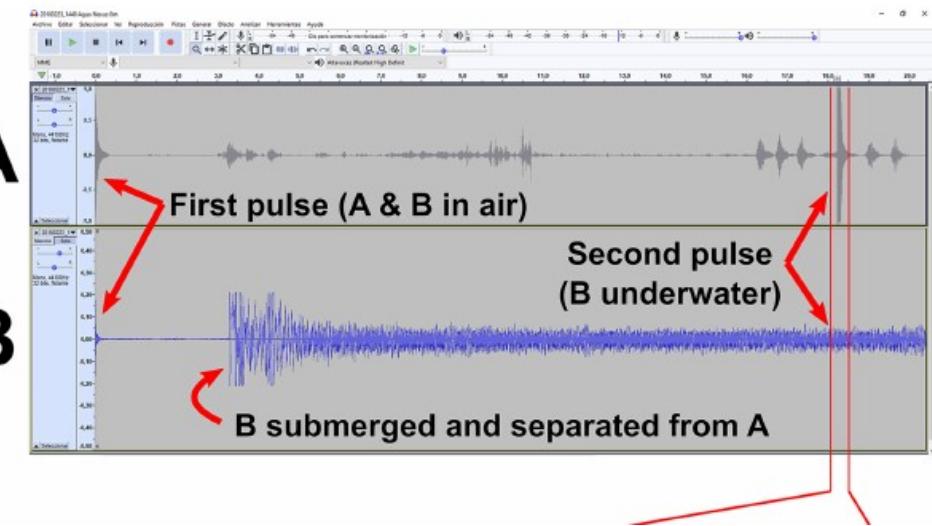
Phys. Educ. 55 (2020) 033013 (4pp)

## Using smartphones as hydrophones: two experiments in underwater acoustics

Martín Monteiro<sup>1,2</sup>  and Arturo C Martí<sup>2</sup> 



Medio “extraño” ruidoso  
Dificultades para medir

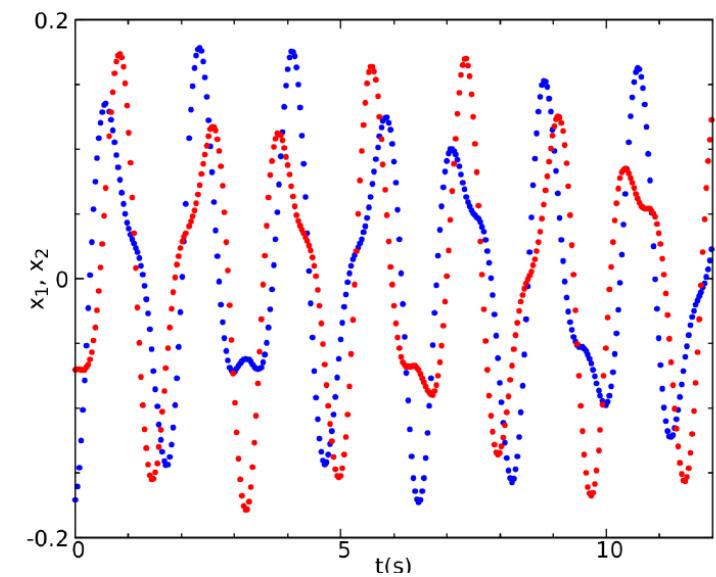
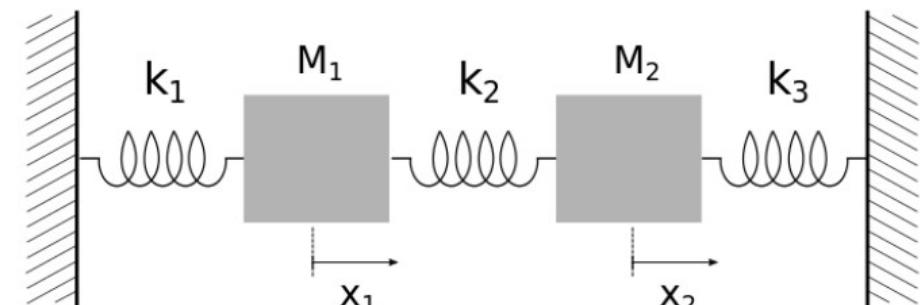
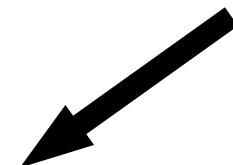
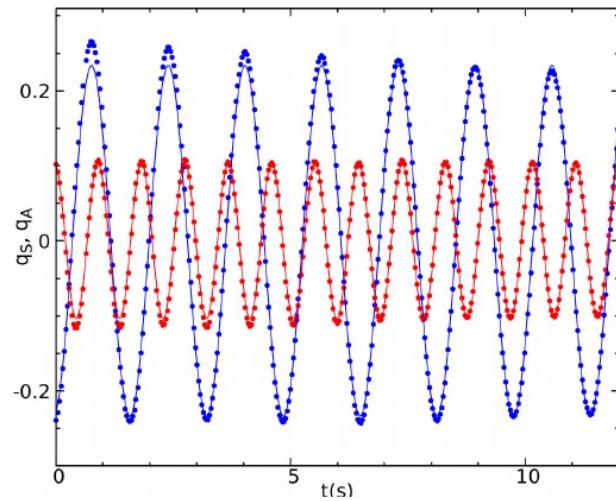


# T6: ver *directamente* los modos normales

Los modos normales son un *artificio* matemático?

En un sistema oscilando en forma arbitraria cómo podemos *ver* los modos normales?

Cómo influye la masa de los resortes?



A. Suárez, D. Baccino, MM, AM,  
enviado 2020

# T7: enseñanza de la energía

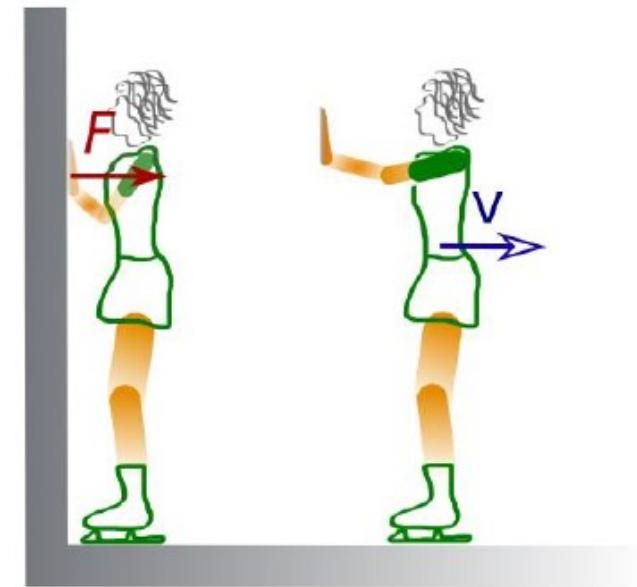
Los enfoques tradicionales que nos enseñaron sobre energía tienen inconsistencias cuando se toma en cuenta la energía interna

Se vienen publicando artículos hace muchos años

Apenas han repercutido en algunos medios....

*Inconsistencies and errors in traditional approaches  
to energy in our introductory courses*

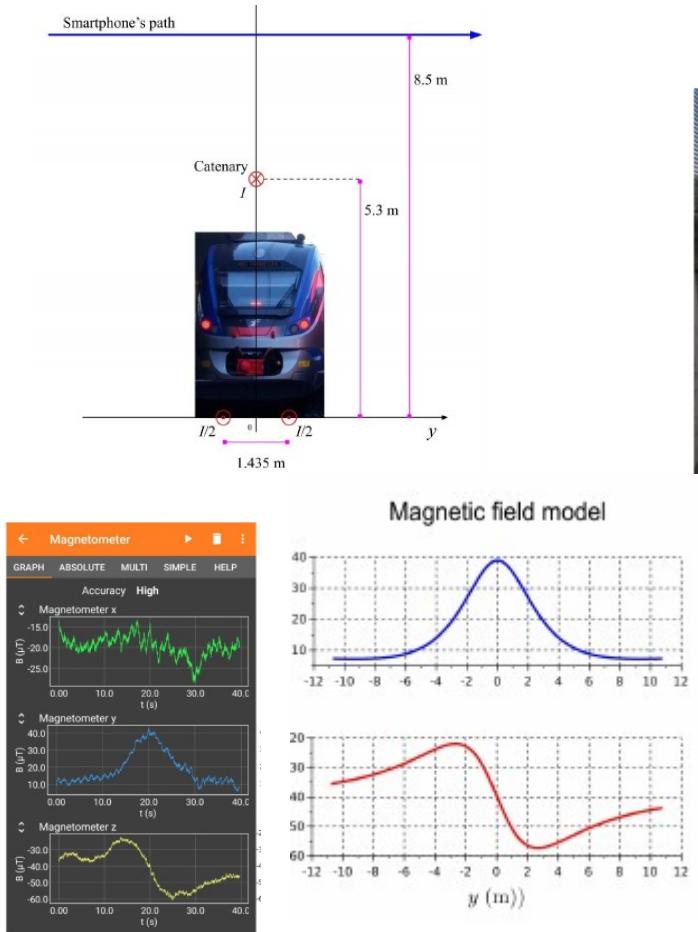
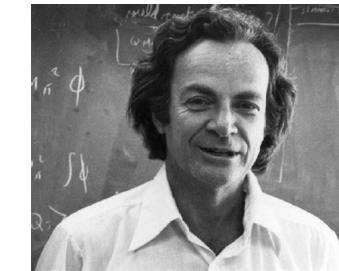
Álvaro Suárez, Daniel Baccino,  
Arturo C. Martí, Martín Monteiro



**A. Suárez, D. Baccino, MM, AM,  
enviado 2020**

# T8: campo magnético de trenes

Try to imagine what the electric and magnetic fields look like at present in the space in this lecture room. First of all, there is a steady magnetic field; it comes from the currents in the interior of the earth—that is, the earth's steady magnetic field. Then there are some irregular, nearly static electric fields produced perhaps by electric charges generated by friction as various people move about in their



**MM, Giovanni Organtini, AM,  
aceptado 2020**

# T9: fluctuaciones y sensores

An Approach to Teach Error Analysis and Uncertainties based on Mobile-device Sensors

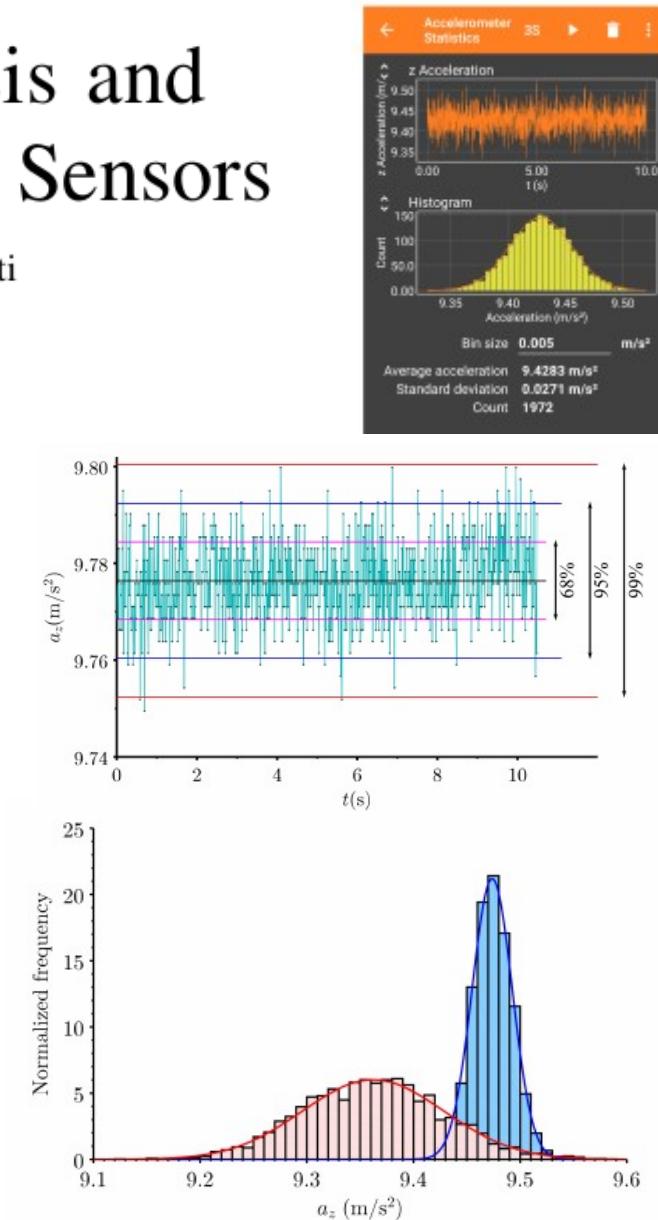
Martin Monteiro, Cecilia Stari, Cecilia Cabeza, and Arturo C. Martí

**Los sensores presentan fluctuaciones alrededor del valor medio**

**Estas fluctuaciones son muy útiles para estudiar errores tipo “A”.**

**Es posible hacer en pocos segundos las prácticas que antes nos llevaban mucho tiempo**

**El conocimiento de las fluctuaciones puede aplicarse a diversos problemas**



# T10: memoria y SW

## Small-worldness favours network inference in synthetic neural networks

Rodrigo A. García\*, Arturo C. Martí, Cecilia Cabeza & Nicolás Rubido

SCIENTIFIC REPORTS | (2020) 10:2296 | <https://doi.org/10.1038/s41598-020-59198-7>

### Paper reciente de J. García-Ojalvo

[Home](#) > [Chaos: An Interdisciplinary Journal of Nonlinear Science](#) > [Volume 30, Issue 6](#) > [10.1063/5.0009709](#)



NF

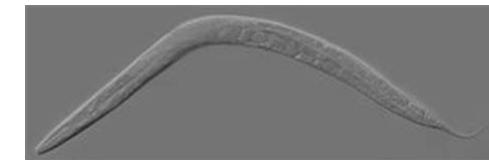
No Access · Published Online: 01 June 2020 Accepted: May 2020

#### Soft-wired long-term memory in a natural recurrent neuronal network

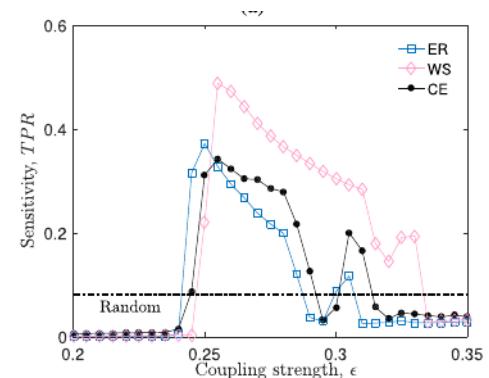
*Chaos* **30**, 061101 (2020); <https://doi.org/10.1063/5.0009709>

Miguel A. Casal<sup>1,2,3</sup>, Santiago Gallella<sup>1</sup>, Oscar Vilarroya<sup>4,5</sup>, and Jordi Garcia-Ojalvo<sup>1,a</sup>

**Memoria a largo plazo y efecto small-world usando modelos sencillos de neuronas**



**SCIENTIFIC  
REPORTS**  
nature research



# The peculiar organization of the trajectories in the Mackey-Glass delayed model.

TRANSACTIONS ON CIRCUITS AND SYSTEMS I: EXPRESS BRIEFS

TRANSACTIONS ON CIRCUITS AND SYSTEMS I, VOL. X, NO. Y, —

## Exact Discrete-time Implementation of the Mackey-Glass Delayed Model

Pablo Amil, Cecilia Cabeza, Arturo C. Martí

CHAOS 25, 043112 (2015)

## Organization and identification of solutions in the time-delayed Mackey-Glass model

Pablo Amil,<sup>1</sup> Cecilia Cabeza,<sup>1</sup> Cristina Masoller,<sup>2</sup> and Arturo C. Martí<sup>1</sup>

# Mackey-Glass model (1977)

Oscillation and Chaos in Physiological Control Systems



Michael C. Mackey, Leon Glass

Science, New Series, Volume 197, Issue 4300 (Jul. 15, 1977), 287-289.

- Respiratory and hematopoietic (formation of blood cellular components) diseases
- The production rate is not constant but depends on the state of the system at some previous time.
- There is delay between the initiation of cell production and the release into the blood.

$$\frac{dx}{dt} = \beta \frac{x_\tau}{1 + x_\tau^n} - \gamma x$$

Production rate      Delay       $x_\tau = x(t - \tau)$       Decay rate

A diagram showing the components of the Mackey-Glass differential equation. The equation is  $\frac{dx}{dt} = \beta \frac{x_\tau}{1 + x_\tau^n} - \gamma x$ . Arrows point from the terms to their labels: a double-headed arrow from  $\beta \frac{x_\tau}{1 + x_\tau^n}$  to 'Production rate' and 'Delay'; a double-headed arrow from  $-\gamma x$  to 'Decay rate'. Below the equation, the term  $x_\tau = x(t - \tau)$  is written.

# Looks simple but....

- First-order differential delay equation (DDE)
- Initial condition: all the interval  $(-\tau, 0)$
- Figures 3-12: Time delay embedding of slides initially presented at the November 1977 New York Academy of Sciences meeting.  $x(t - 2)$  is the ordinate and  $x(t)$  is the abscissa with  $\gamma = 1, \beta = 2$ , and  $\tau = 2$

Recurrence plots

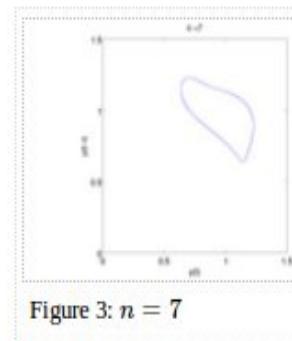


Figure 3:  $n = 7$

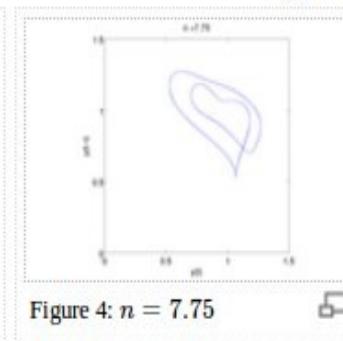


Figure 4:  $n = 7.75$

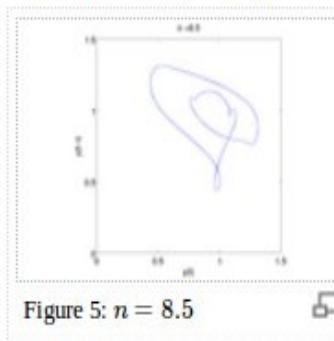


Figure 5:  $n = 8.5$

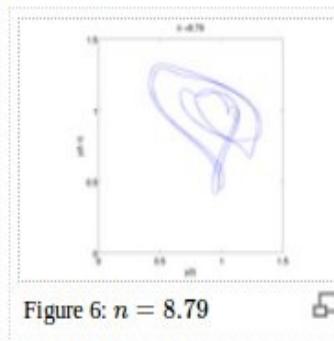


Figure 6:  $n = 8.79$

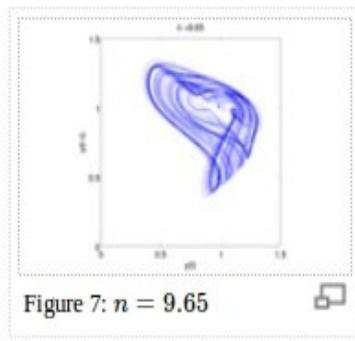


Figure 7:  $n = 9.65$

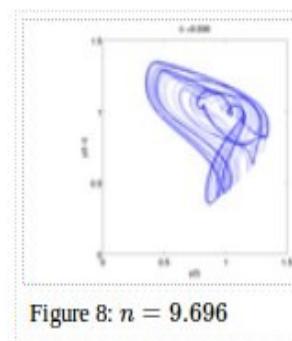


Figure 8:  $n = 9.696$

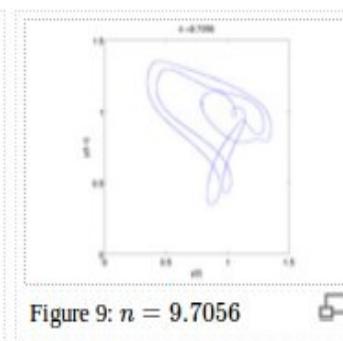


Figure 9:  $n = 9.7056$

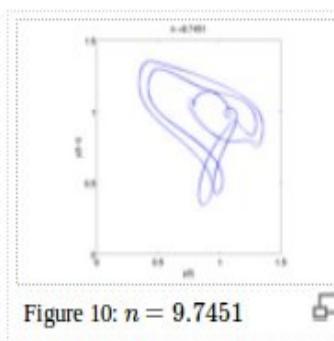


Figure 10:  $n = 9.7451$

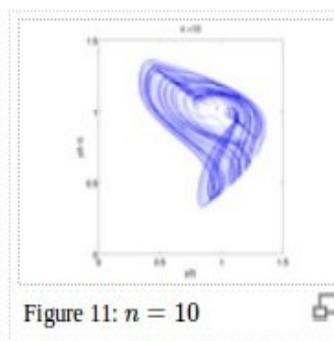


Figure 11:  $n = 10$

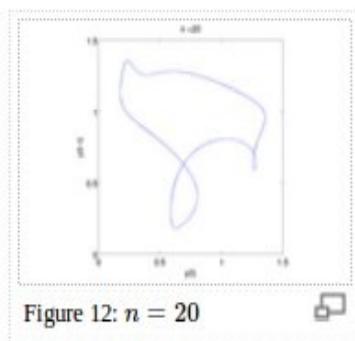


Figure 12:  $n = 20$

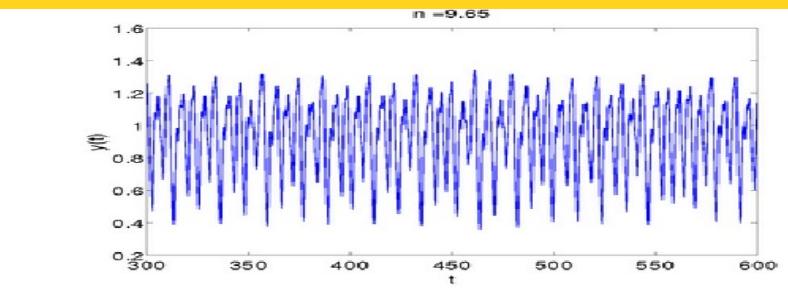


FIG. 2. Time series and return map for the Mackey-Glass equation, (1), for  $\gamma = 1$ ,  $\beta = 2$ , and  $\tau = 2$ ,  $n = 9.65$

# +4000 cites to the original paper

 **Physica D: Nonlinear Phenomena**  
Volume 4, Issue 3, March 1982, Pages 366–393 

**Chaotic attractors of an infinite-dimensional dynamical system**  
**J. Doyne Farmer\***  
Dynamical Systems Group, Physics Dept., U.C. Santa Cruz, Santa Cruz, Ca. 95064, USA

 **Physica D: Nonlinear Phenomena**  
Volume 9, Issues 1–2, October 1983, Pages 189–208 

**Measuring the strangeness of strange attractors**  
**Peter Grassberger<sup>†</sup>, Itamar Procaccia**  
Department of Chemical Physics, Weizmann Institute of Science, Rehovot 76100, Israel

**PHYSICAL REVIEW A** **VOLUME 28, NUMBER 4** **RAPID COMMUNICATI** **OCTOBER 1983**

**Estimation of the Kolmogorov entropy from a chaotic signal**  
**Peter Grassberger**  
Physics Department, University of Wuppertal, D-5600 Wuppertal 1, Germany

**Itamar Procaccia**  
Chemical Physics Department, Weizmann Institute of Science  
(Received)

A new method for estimating the Kolmogorov entropy from time series examples. The method should prove valuable for...



Browse Conference Publications > Adaptive Systems for Signal Processing ... 

**The unscented Kalman filter for nonlinear estimation**

2 Author(s) Wan, E.A.; Oregon Graduate Inst. of Sci. & Technol., Beaverton, OR, USA; Van der Merwe, R.

APS » Journals » Phys. Rev. Lett. » Volume 59 » Issue 8

Phys. Rev. Lett. 59, 845–848 (1987)

## Predicting chaotic time series

Abstract

References

Citing Articles (726)

Page Images

Download: PDF (266 kB) Export: BibTeX or EndNote (RIS)

J. Doyne Farmer and John J. Sidorowich

Theoretical Division and Center for Nonlinear Studies, MS B258, Los Alamos National Laboratory, Los Alamos, New Mexico 87545

Received 22 April 1987; published in the issue dated 24 August 1987

PHYSICAL REVIEW E 75, 016207 (2007)

## Dual synchronization of chaos in Mackey-Glass electronic circuits with time-delayed feedback

Satoshi Sano,<sup>1</sup> Atsushi Uchida,<sup>1,2</sup> Shigeru Yoshimori,<sup>1</sup> and Rajarshi Roy<sup>2,3,4</sup>

<sup>1</sup>Department of Electronics and Computer Systems, Takushoku University, 815-1 Tatemachi, Hachioji, Tokyo 193-0985, Japan

<sup>2</sup>IREEAP, University of Maryland, College Park, Maryland 20742, USA

<sup>3</sup>IPST, University of Maryland, College Park, Maryland 20742, USA

<sup>4</sup>Department of Physics, University of Maryland, College Park, Maryland 20742, USA

(Received 18 August 2006; published 12 January 2007)

We experimentally and numerically demonstrate the dual synchronization of chaos in two pairs of one-way coupled Mackey-Glass electronic circuits with time-delayed feedback. The outputs of the two drive circuits are mixed and used both for the feedback signal to the two drive circuits and for the transmission signal to the two response circuits. We investigate the regions for achieving dual synchronization of chaos when the delay time

Contents lists available at SciVerse ScienceDirect

## Physics Letters A

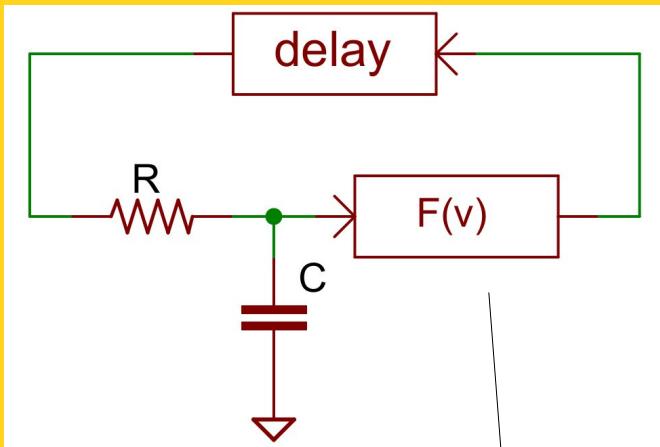
[www.elsevier.com/locate/pla](http://www.elsevier.com/locate/pla)



Intricate routes to chaos in the Mackey-Glass delayed feedback system

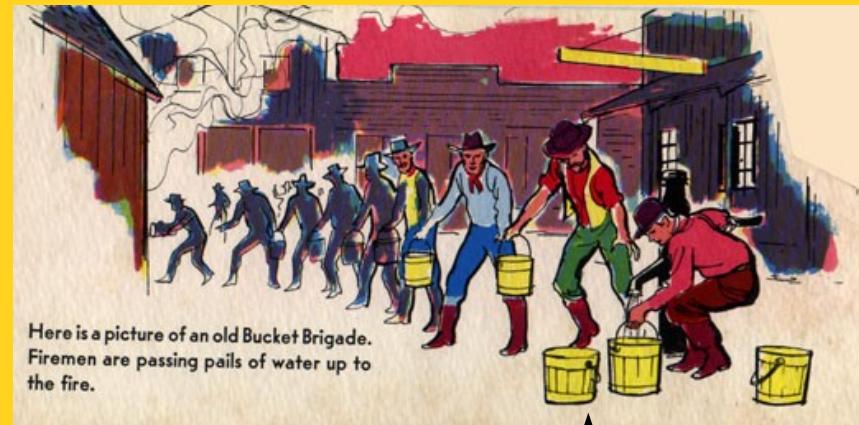
Leandro Junges <sup>a,b</sup>, Jason A.C. Gallas <sup>a,b,c,\*</sup>

# Our experiment: Electronic implementation



Function block →  
“arbitrary” nonlinear  
function

Bucket bridge device: analogy with the term *bucket brigade*, (line of people passing buckets of water)

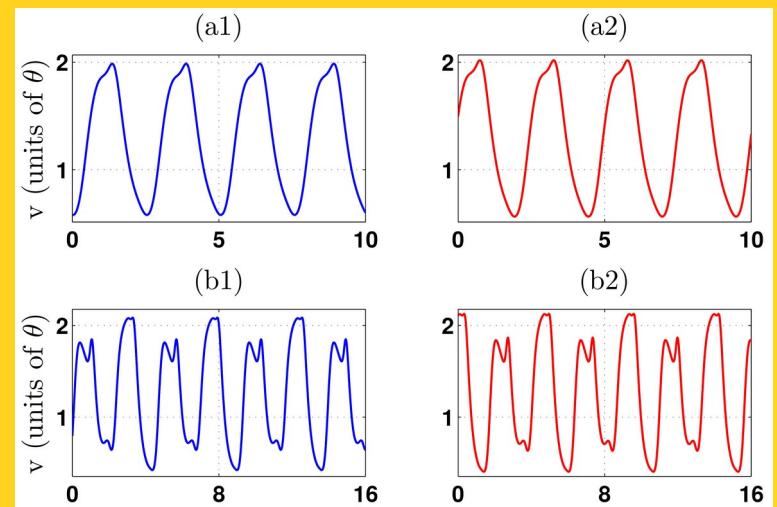


- Pre and post amplification → low noise
- Analog voltage, discrete time
- Effective equation → exact temporal integration
- Continuous limit → original equation

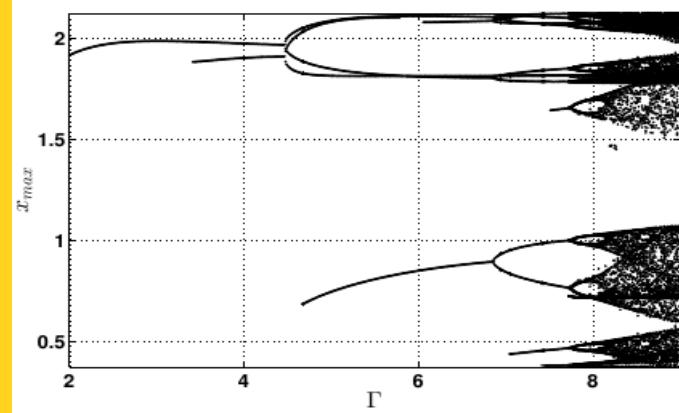
$N \sim 1000$

# Bifurcation diagrams

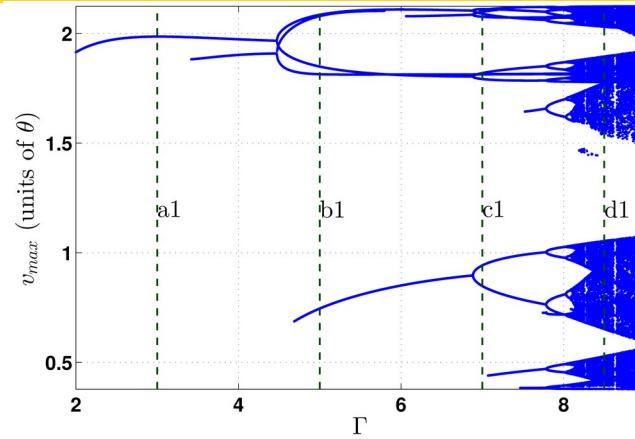
- Maxima of the temporal series
- Increasing the time-delay



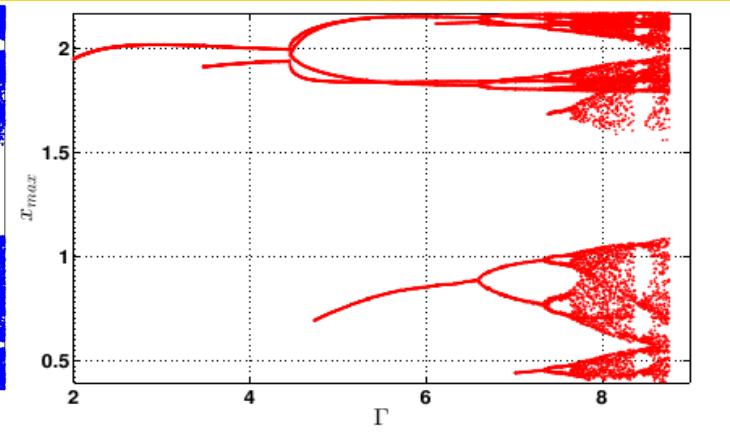
Original equation:



Discrete equation:

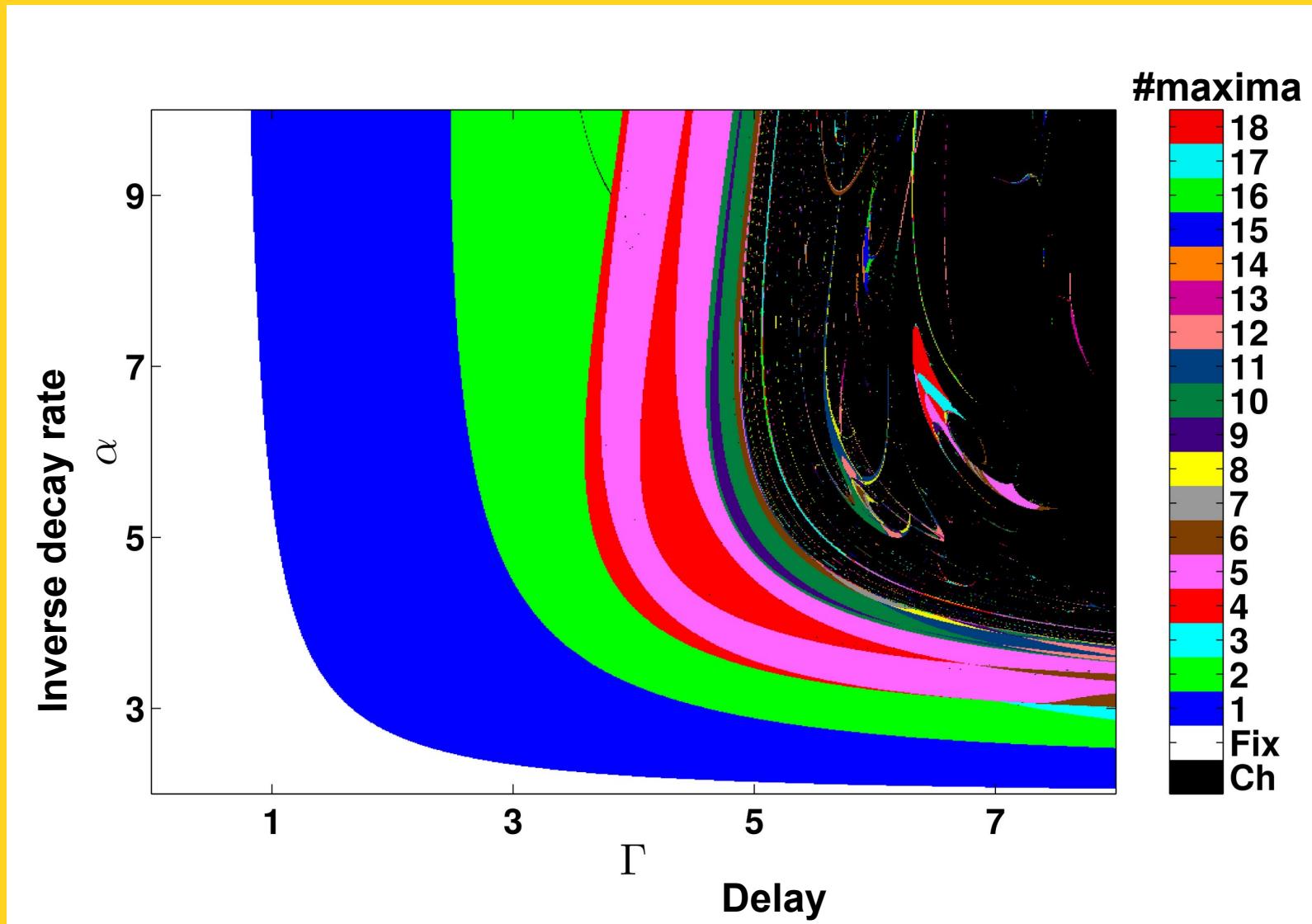


Experimental:



- Period doubling
- Isolated branches (begin or end abruptly)!!!
- Particular of DDEs.

# Periodicity in the parameter space

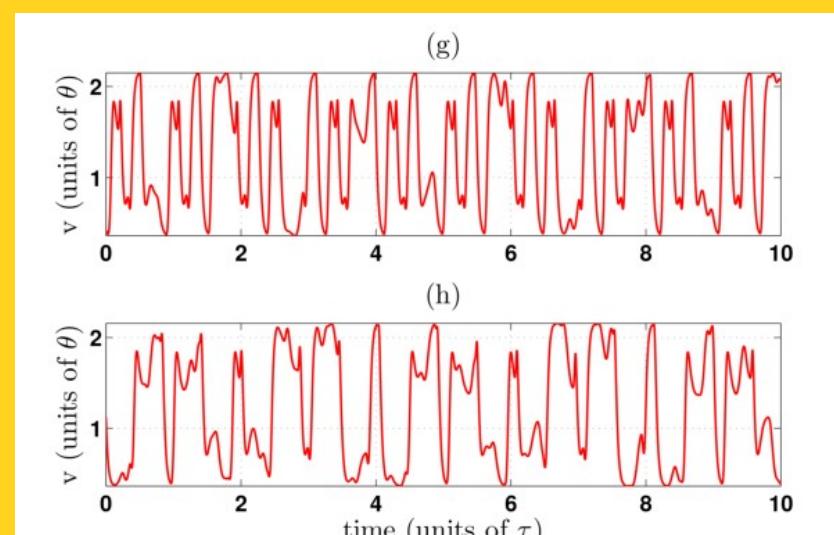
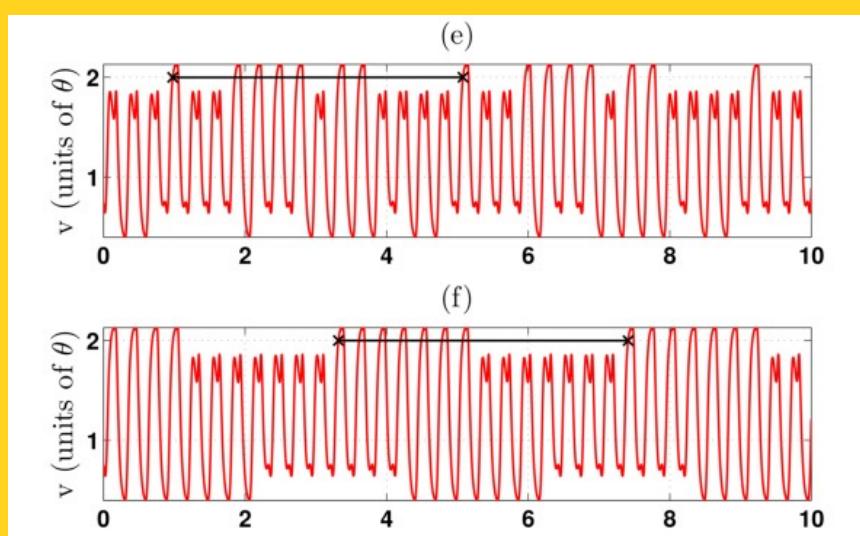
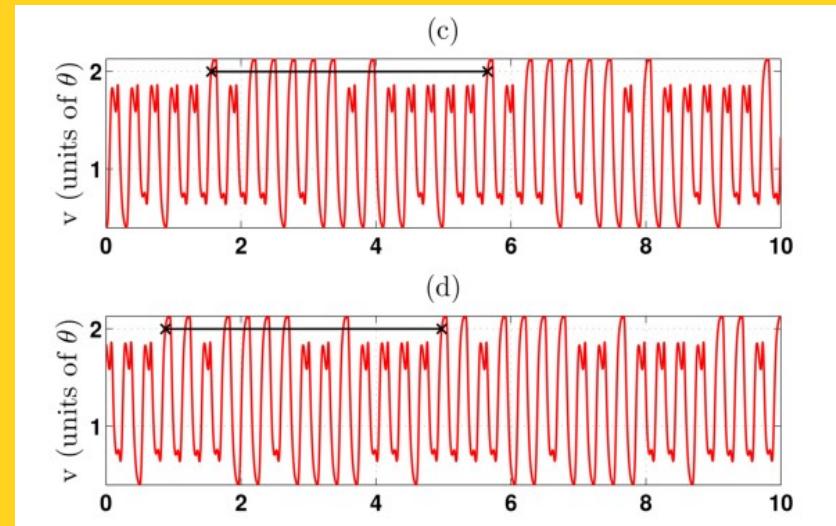
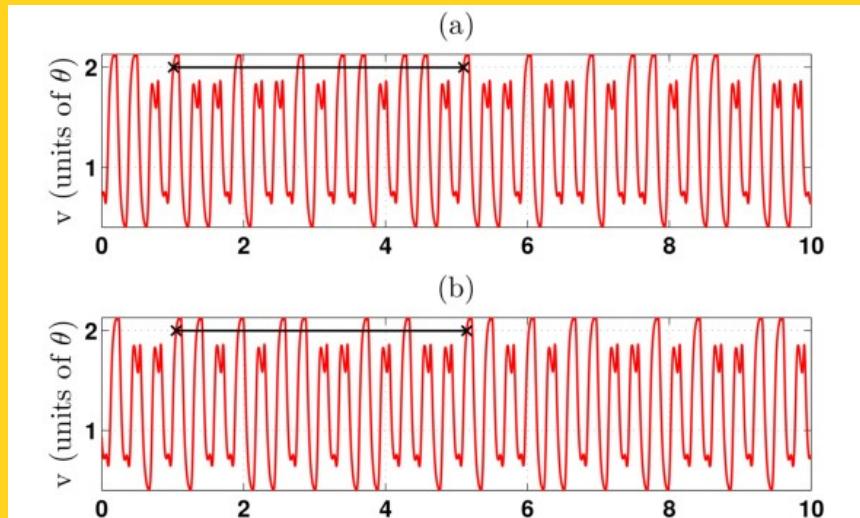


# Multistability

Different initial functions (IFs)

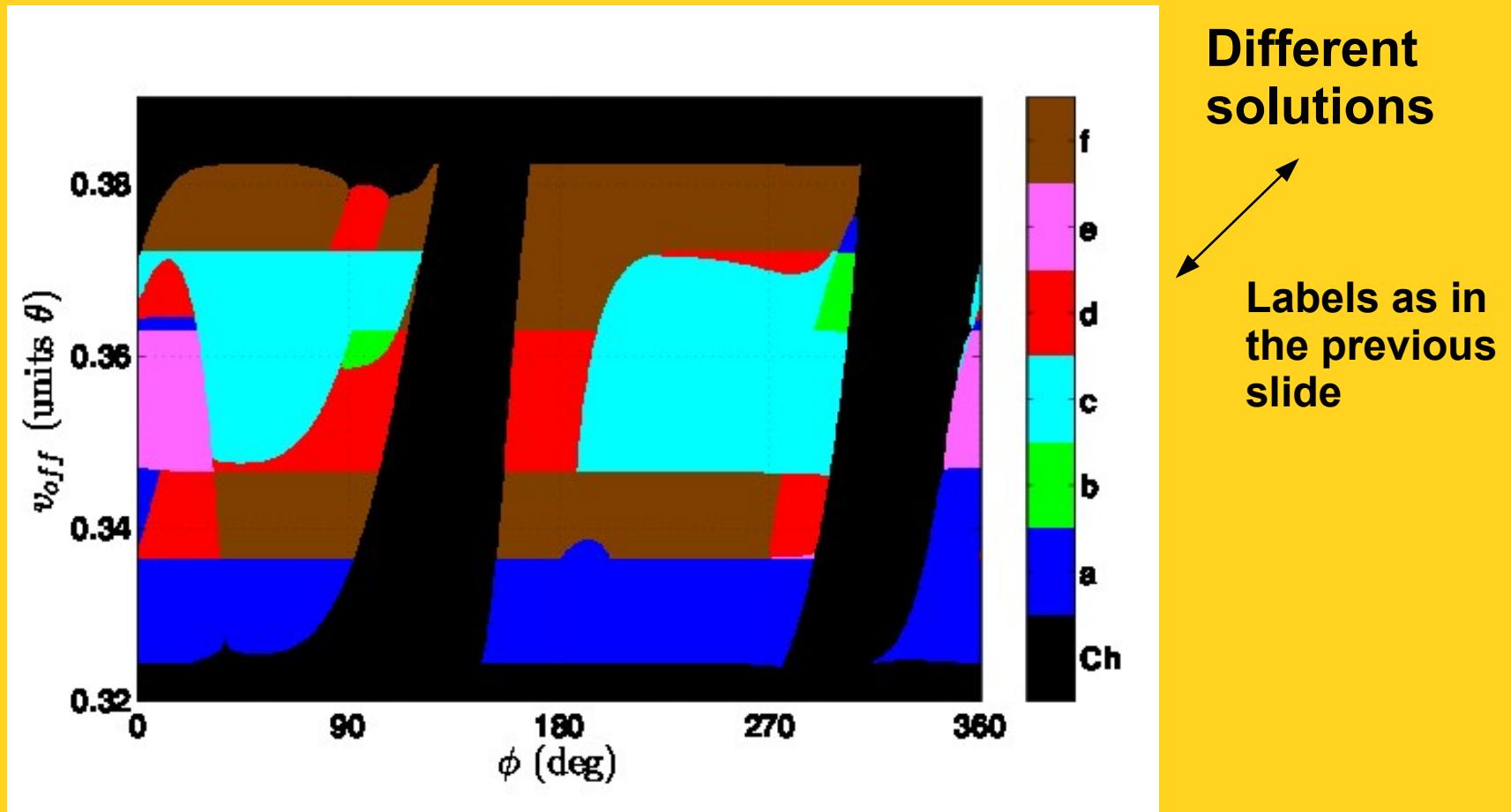
$$F_0(t) = \frac{1}{40} \sin\left(\frac{7\pi t}{2\tau} + \phi\right) \sin\left(\frac{7\pi t}{\tau} + 2\phi\right) + v_{\text{off}},$$

Coexistence of different solutions (different alternations of peaks)



# Initial conditions space

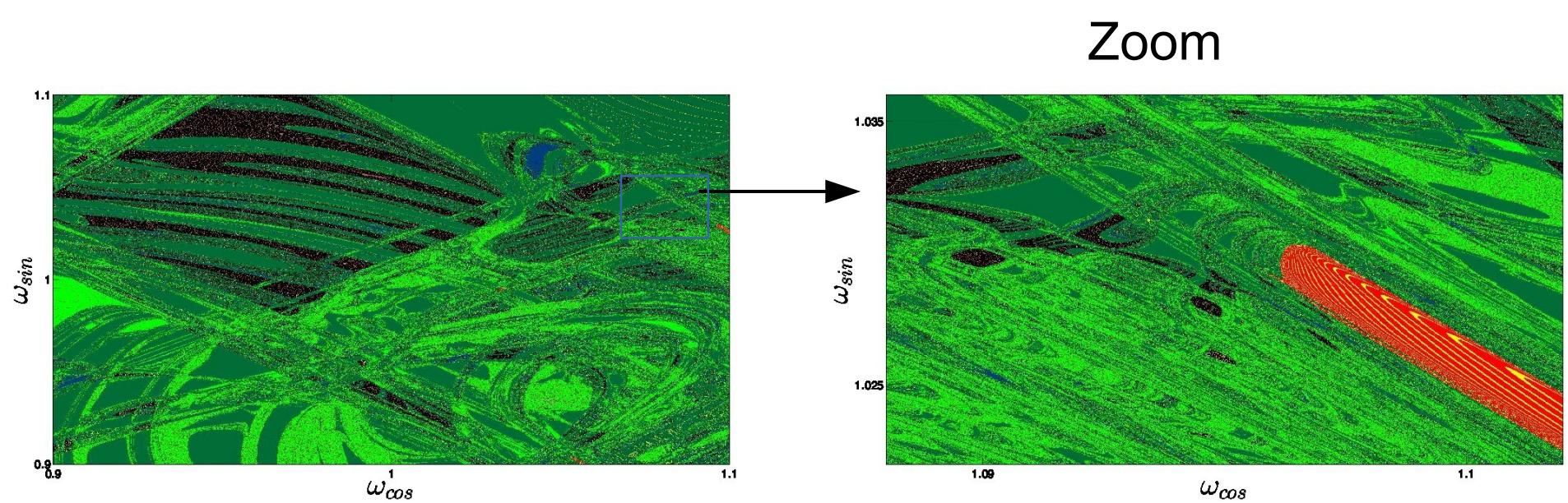
Symbolic algorithm to classify the solutions:



$$F_0(t) = \frac{1}{40} \sin\left(\frac{7\pi t}{2\tau} + \phi\right) \sin\left(\frac{7\pi t}{\tau} + 2\phi\right) + v_{off},$$

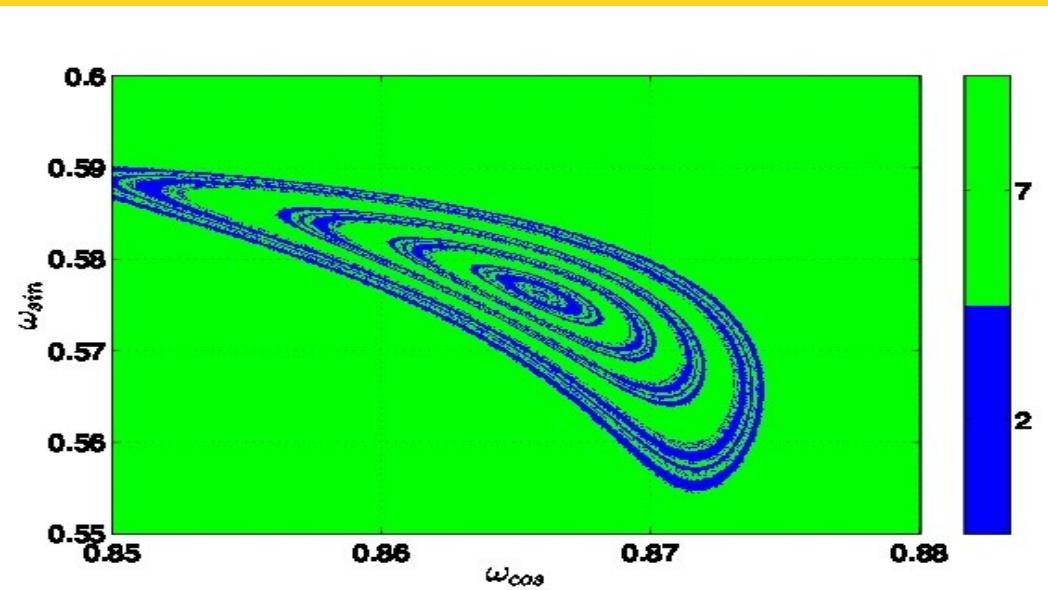
# Seudo-random initial functions

$$F_0 = 2 + \sin(\omega_{\sin} 2\pi t/\tau) + \cos(\omega_{\cos} 2\pi t/\tau).$$

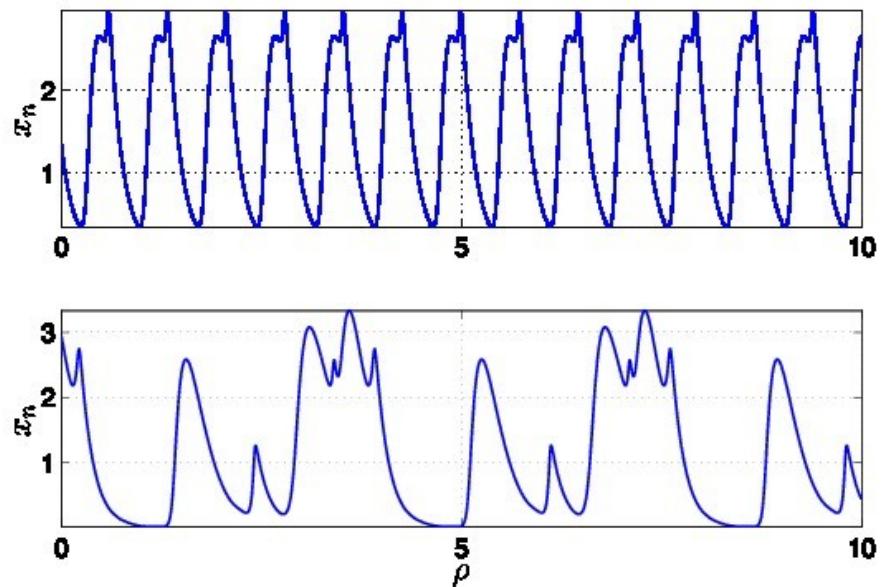


Different initial conditions  
Colors indicate number of maxima (black chaos)

# More structures:



$$F_0 = 2 + \sin(\omega_{sin} 2\pi t / \tau) + \cos(\omega_{cos} 2\pi t / \tau).$$

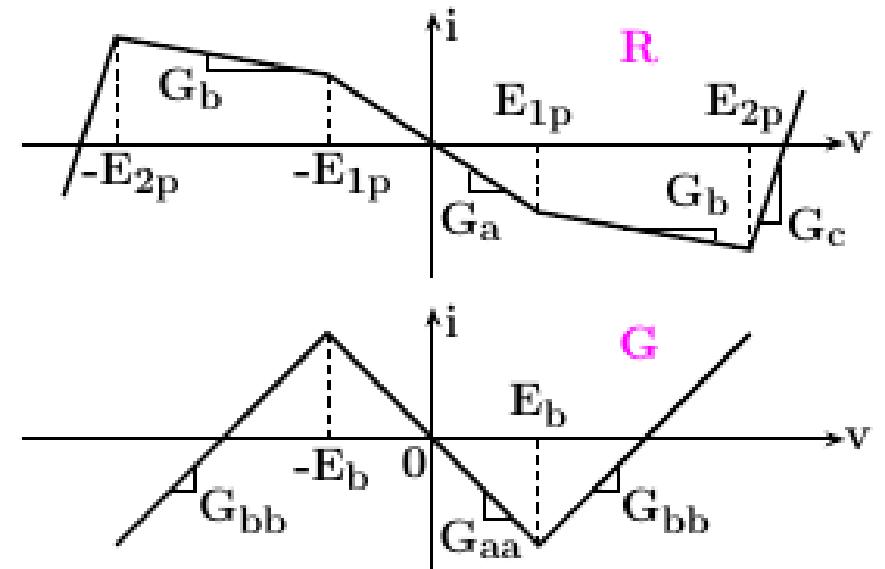
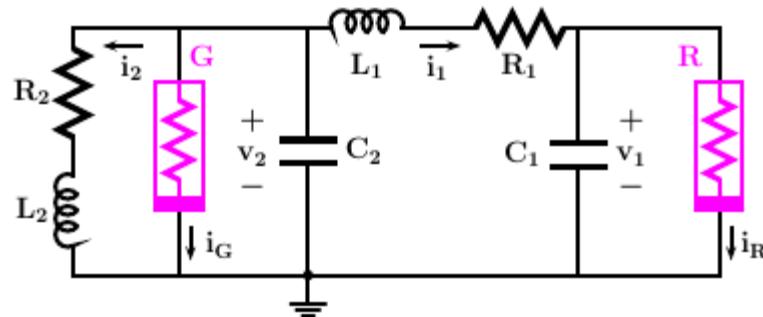


# Comentarios:

- Electronic system with time delay mimicking MG model
- Exact temporal evolution
- Coexistence of different solutions (equal period, different alternation of peaks)
- Peculiar organization in the initial condition space
- Robust to noise and parameter mismatch
- Isospike diagrams do not fully characterize the behavior.
- Applications: memory storage? pattern recognition?

# T11": sistemas con retardo, nuevos estudios

## Resistencias no lineales



## Modelo de Mackey-Glass con resistencia no lineal

# Gracias por su atención!